

**University of Macau**

**Faculty of Science and Technology**

**Department of Mathematics**

**FST-SEM/00082/2015**

**Hodge-Dirac Operators in  $L_p$  Spaces on Lipschitz Domains**

BY

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**Date: 28 September 2015 (Monday)**

**Time: 10:00 a.m. - 11:00 a.m.**

**Venue: E11- 1012**

**Abstract**

The Hodge–Dirac operator  $DH = d\Omega + d\Omega^*$  on a bounded domain  $\Omega \subset \mathbb{R}^n$  is self-adjoint in  $L^2(\Omega)$ , and so has bounded resolvents and bounded functional calculi. I shall discuss the question as to when the resolvents and functional calculi are bounded in  $L_p(\Omega)$  for some range of values of  $p \in (p_H, p_H)$ , where  $p_H < 2 < p_H$ .

The square of the Hodge–Dirac operator is the Hodge–Laplacian  $\Delta H = DH^2$ , so it has a bounded functional calculus for the same range of values as  $DH$ . But an operator such as the Hodge–Stokes operator, which is the restriction of  $\Delta H$  to a subspace such as the divergence free vector fields, can have a bounded functional calculus on a larger range of values of  $p$ . I shall discuss recent joint research with Sylvie Monniaux (Marseille) on this topic.

**Biography**

Alan McIntosh is a famous mathematician who solved, with Coifman and Meyer together, the long standing boundedness problem of the Cauchy singular operator on Lipschitz curves, the so called CMcM theorem. He is also a contributor to the solution of Kato's conjecture. Alan is Fellow of The Australian Academy, was director of Center of Mathematical Analysis and Applications, Australian national University, Canberra. Before that he was Professor at Macquarie University, Sydney.

**All are Welcome!**

FST Seminar - MAT - "Hodge-Dirac Operators in  $L_p$  Spaces on Lipschitz Domains" at 10:00am on 28 September 2015 (Monday), E11-1012